

Designing Drive Systems for Low Web Speed Applications

William B. Gilbert
Converting Solutions
Siemens Industry, Inc.
5300 Triangle Parkway, Suite 100
Norcross, GA 30092
Phone: 770.625.5658
Fax: 770.871.3888
Email: William.Gilbert@Siemens.com
Website: www.siemens.com/converting

Table of Contents

<i>Abstract</i>	3
<i>Design Considerations</i>	3
Tension Control Modes	3
Determining the Tension Control Mode	5
Drive Sizing	5
Gearbox Efficiency	5
Reference Machine Example	6
System Design (Unwind / Rewind)	7
Issues with High Ratio Gearing	8
An Alternative Solution	9
<i>Conclusions</i>	10
<i>References</i>	10

Abstract

The low web speeds of roll to roll sputtering technology metallizers can pose interesting challenges to the effective design of the electrical and mechanical drive system. With typical web speeds in inches per minute, the drive power requirements are commonly very low, even with substrates that demand very high tensions. The traditional solution has been to optimize the power requirements with high ratio gearboxes, in which the gearbox ratios can exceed 100:1 or more.

The physical properties of low compliance substrates such as metals and foils typically dictate that tension control is best achieved by regulating the torque of the driving motor rather than its speed. With high gearbox ratios, the substantial losses can isolate the motor from the load making it difficult to utilize torque regulated tension control.

This paper will look at the solutions that current drive and motor technology can offer in not only improving tension control but also solving several other issues that are inherent to systems with high ratio gearing.

Design Considerations

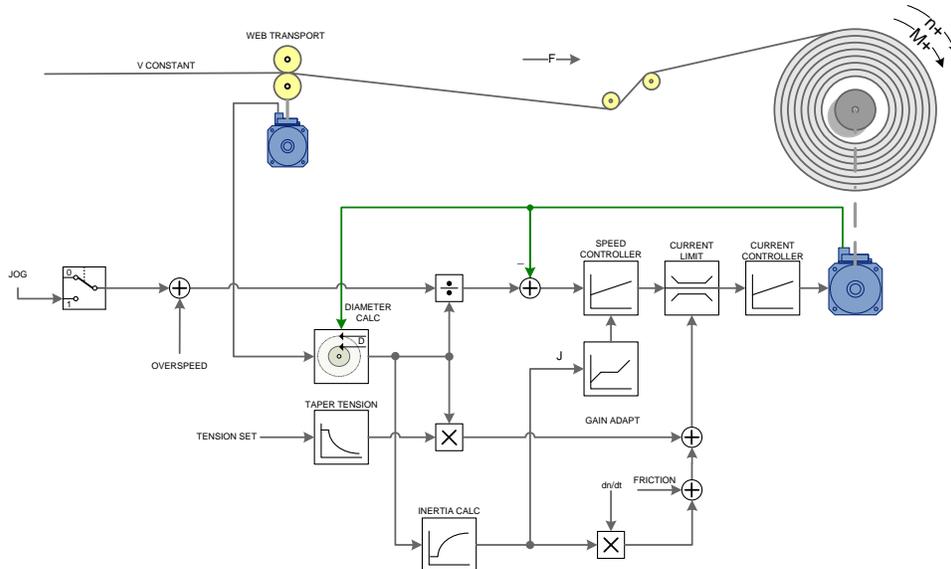
Tension Control Modes

Center driven winders can be operated in one of three modes of tension control.

1. Indirect Torque Control.
2. Torque Limiting Control.
3. Speed Setpoint Correction Control.

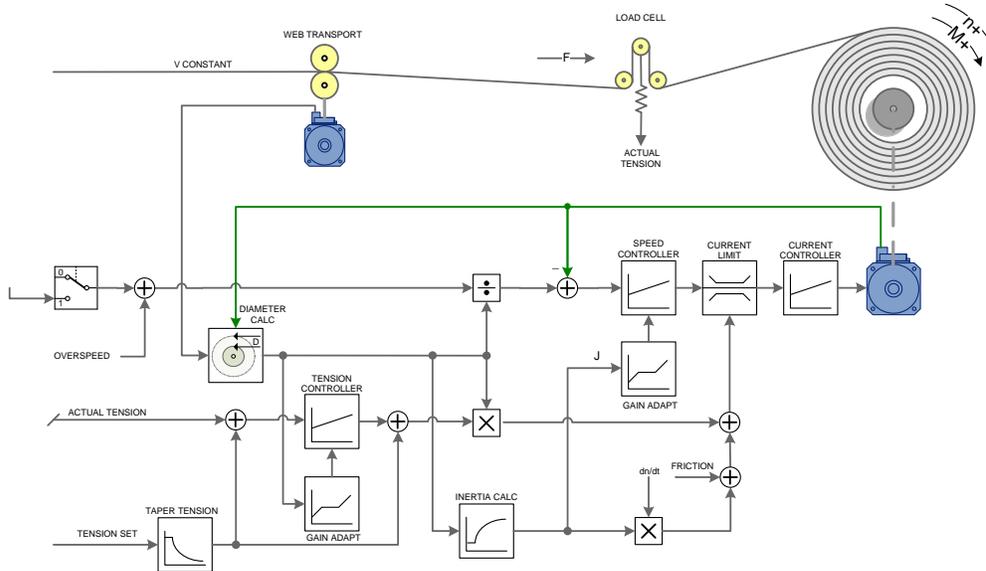
Indirect Tension Control is technically the simplest, but the least accurate of the modes. Indirect control does not make use of a tension feedback sensor. The tension control is open loop, directly based on the tension setpoint, factored by a measured or calculated diameter. Inertia and friction compensation can be a control feature of this mode.

Figure 1: Indirect Torque Control



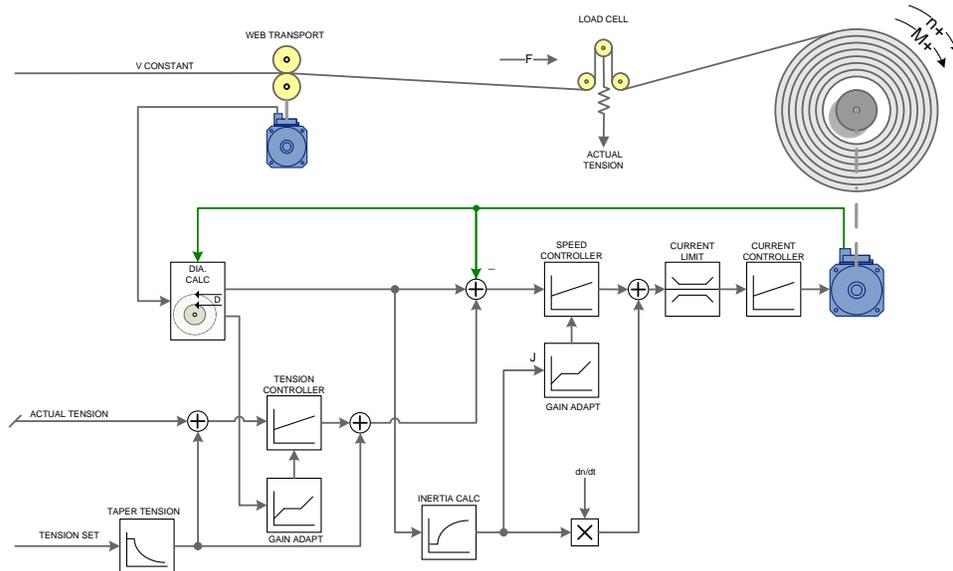
Torque Limiting Tension Control is closed loop, based on the tension setpoint reference, factored by the actual diameter and compensated by the actual tension error through a PI (tension) control loop as a rotational force. Inertia and friction compensation are normally a control feature of this mode.

Figure 2: *Torque Limiting Control (with load cell sensing)*



Speed Setpoint Correction Tension Control is closed loop, based on the actual web speed reference, factored by the actual diameter and compensated by the transformed tension error through a PI (tension) control loop as a speed setpoint addition. Inertia and friction compensation can be a control feature of this mode.

Figure 3: *Speed Setpoint Correction Control (with load cell sensing)*



Determining the Tension Control Mode

The selection of the winder tension control mode can be influenced by several factors including machine specifications or design, the type of tension sensor used if any, but normally the major determining factor will be the compliance of the web material being transported.

The modes of torque control are commonly adapted when the web material has a very low compliance or is “non-extensible”, e.g. heavy paper, steel, aluminum or other metals. With a non-compliant web, the increased system gain of a speed controlled system will make the system tend towards instability and much more complex to optimize tuning. The current or torque regulated modes of control tend to be more stable over a wider range of conditions. When implementing the torque modes, consider torque limiting with tension feedback if accuracy is important.

The mode of tension regulation via speed control is ideally implemented when the web is highly compliant or “extensible”. In this mode, the added system gain from additional control loop (speed controller) and the transformation from force (load cell) to speed (speed loop) to torque (current loop) help with the additional system demands.

Drive Sizing

In the engineering and design of web handling drive systems the traditional practice is to optimize the drive and motor sizes as close as possible to the web power requirement. This is accomplished by selecting a mechanical gear ratio that will enable the motor to run as close as possible to its base speed in a web transporting driven section (non-winder), and well into the constant power range for center driven winder or unwind (when an induction motor is used).

The optimum gear ratio is determined by;
Optimum Motor Speed RPM / Maximum Load Speed RPM

For a driven section with a fixed diameter roll the power requirement is determined by the maximum torque requirement at the maximum speed. The power requirements for a fixed diameter transporting roll (sectional drive / pull roll) come from the following;

$$\text{Max Torque (lbf-in)} = ((\text{Driven Roll Diameter (in.)} / 2) * \text{Maximum Web Tension (lb.)} / (\text{Gear Ratio} * \text{Gearing Efficiency}))$$

$$\text{Max Speed (RPM)} = \text{Maximum Web Speed FPM} / ((\pi * \text{Driven Roll Diameter (in.)} / 12) * \text{Gear Ratio})$$

The work done by center driven winders or unwinds is constant power. The torque and speed requirements change throughout the building of the roll. The torque is the highest at full roll with the speed the lowest. At the core or smallest diameter, the speed is the highest and the torque is the lowest. We can consider the following as the main sizing criteria for a center driven unwind or rewind;

$$\text{Max Torque at Full Roll (lbf-in)} = ((\text{Full Roll Diameter (in.)} / 2) * \text{Maximum Web Tension (lb.)} / (\text{Gear Ratio} * \text{Gearing Efficiency}))$$

$$\text{Max Speed at Core (RPM)} = \text{Maximum Web Speed (FPM)} / ((\pi * \text{Core Diameter (in.)} / 12) * \text{Gear Ratio})$$

Gearbox Efficiency

The gearbox selection will determine efficiency factor component of the torque calculations. Gearbox efficiency is simply the ratio of the output power (power transmitted through the gearbox as usable work) to the input power. As no mechanical device is 100% efficient, this numeric value of efficiency will always be less than 1. If a speed reducer were 100% efficient, all of torque being applied to the input shaft would be applied to the output shaft.

$$\text{Gearbox Efficiency} = (\text{Actual Output Torque} / \text{Theoretical Output Torque}) * 100$$

Typical gearing options are Planetary, Helical, Worm and Pulley / Timing belt. Generally planetary gear boxes are limited to 100:1 ratio, with about a maximum ratio of about ~8:1 per stage (there are some exceptions to this rule). Efficiencies for planetary gearing can be considered at ~90- 95% per stage.

For gear ratios over 100:1, the options are typically multistage worm, helical or combination gearboxes. See figure 4 for a reference of general efficiencies for multistage gearboxes with ratios greater than 100:1 and figure 5 for general efficiencies for planetary gearboxes.

Figure 4: Typical Multi-stage High Ratio Gearbox Efficiency

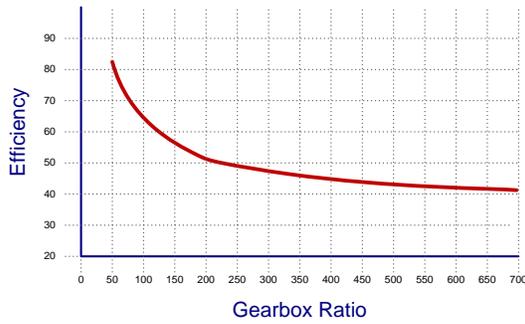
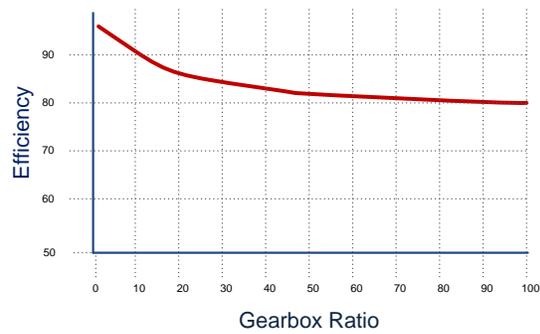


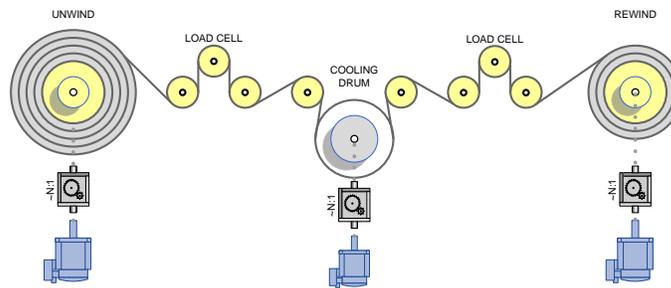
Figure 5: Typical Planetary Gearbox Efficiency



Reference Machine Example

Consider a machine with three driven sections, an unwind, a cooling drum as the master and web transport and a winder. The cooling drum is the system master and is responsible for transporting the web. The unwind and winder spindles are tension controlled with tension feedback from load cell transducers. The web material being transported is a stainless steel foil. Since the web is non-extensible, the mode of tension control for the spindles will be configured as direct torque control.

Figure 6: Example Machine Configuration



Example Machine Specifications:

WEB TENSION		
Min.	1.00	Pli
Max.	10.00	Pli

MATERIAL / SPINDLE		
Core	6.75	in.
Full	20.00	in.

LINE SPEED		
Min.	0.25	Fpm
Max.	3.00	Fpm
Jog	12.00	Fpm

COOLING ROLL		
Dia.	42.0	in.
Weight	2000.0	lb.

WEB WIDTH		
Min.	6.00	in.
Max.	14.00	in.

Power requirements or Web HP from the above specifications would be analyzed in the following manner;
 Max Web HP = (10 PLI * 14 inches) * 12.00FPM / 33,000 = 0.1508HP

Considering the very low power requirements of this system and that the industry tend to use synchronous servo motors in the drive systems when power requirements are at fractional HP and below , we will consider synchronous servo motors for each axis. This type of motor/ drive system fits with industry practice. Servo motors in this size range will typically have a rated or maximum speed of 4500 RPM to 6000RPM.

Instead of considering power as the sizing criteria, the following sizing examples will select motors based on the criteria of maximum torque requirements at the full roll max tension and the maximum speed requirement at max speed at core. Since the master (cooling drum) will be speed regulated, and the system lead section, the following exercises with concentrate only on the unwind and rewind spindles.

System Design (Unwind / Rewind)

Step 1: Determine the spindle gear ratios (for a power optimized system).

From the max RPM at the load and the motor base speed we can determine an optimum gear ratio for a power optimized system.

$$\text{Max RPM @ Core} = \text{Max FPM} / (\Pi * (\text{Core Dia.} / 12)) = 12.00 / (\Pi * (6.75'' / 12)) = 6.79 \text{ RPM}$$

Considering a 4500 RPM motor we find an optimized Gear Ratio = 4500RPM / 6.79 RPM = 662.73:1
For this example we will consider a gearbox ratio of 650:1. This ratio will set the speed at the motor.

$$\text{Max Motor Speed at Core (RPM)} = \text{Maximum Web Speed} / ((\Pi * \text{Core Diameter}'' / 12) * \text{Gear Ratio}) \\ 12.00 \text{ fpm} / ((\Pi * 6.75'' / 12) * 650.00) = 4413.90 \text{ RPM}$$

$$\text{Min Motor Speed at Full roll (RPM)} = \text{Maximum Web Speed} / ((\Pi * \text{Core Diameter}'' / 12) * \text{Gear Ratio}) \\ 0.100 \text{ fpm} / ((\Pi * 20'' / 12) * 650.00) = 31.04 \text{ RPM}$$

Choices for gearboxes in the range of 650:1 are limited and will require the selection of a multi-stage gearbox to achieve a ratio of that magnitude. We can consider that the typical efficiency of a multi stage gearbox with a ratio of 650:1 will be in the area of ~33%.

Step 2: Determine the spindle torque requirements.

$$\text{Max Torque at Core (lbf-in)} = ((\text{Core Diameter} / 2) * (\text{Maximum Web Tension} / (\text{Gear Ratio} * \text{Gear Efficiency}))); \\ ((6.75'' / 2) * (140 \text{ lb.} / (650 * 0.33))) = 2.20 \text{ lbf-in}$$

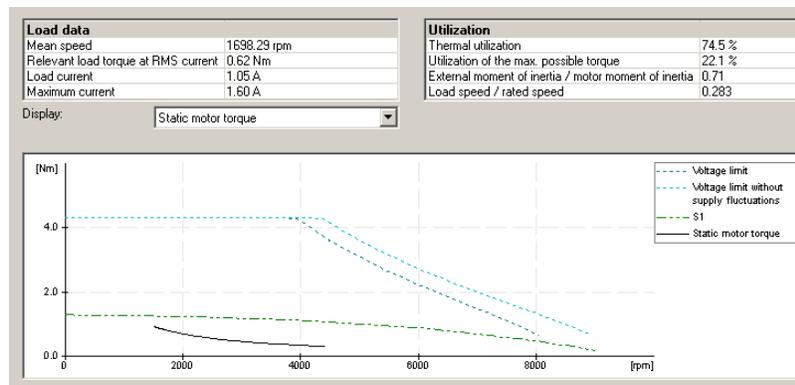
(Note: a system with 90% efficiency would require .807 lbf-in at core)

$$\text{Max Torque at Full Roll (lbf-in)} = ((\text{Full Roll Diameter} / 2) * (\text{Maximum Web Tension} / (\text{Gear Ratio} * \text{Gear Efficiency}))); \\ ((20'' / 2) * (140 \text{ lb.} / (650 * 0.33))) = 6.53 \text{ lbf-in}$$

(Note: a system with 90% efficiency would require 2.39 lbf-in)

With these load criteria we can consider a synchronous motor with the minimum of 2.20 lbf-in of torque at the maximum speed at core and 6.53 lbf-in of torque at minimum speed @ full roll. Based on the data, we select a standard motor rated for (1.3Nm) 11.5 lbf-in at 6000RPM. See figure 7 for the selected motor / load curves.

Figure 7: Motor Selection / Load Requirements



Issues with High Ratio Gearing

Isolation – Friction Losses

The friction losses of the gearbox related as efficiency in effect isolates the motor from the load. We can see the result of that in how the losses in the high ratio multistage gearbox have increased the motor torque requirements, in effect it has tripled both the motor and drive size from ~2.15 lbf-in to 6.53 lbf-in

Active Torque Control Component to Friction Losses

The ratio of the active torque control component to the friction losses should be considered in the design process. Consider that in closed loop tension control modes, only a small component of the tension control signal is active, or supplied by the tension controller. The majority of the tension setpoint is provided from the setpoint modified by the actual diameter. Normally we can consider the active portion of the tension component signal at about 5% of the tension torque component. Because the friction losses are not static and will with time at a constant speed, they also vary with speed, load, the tension control system has to work through the dynamic peaks and valleys of the losses.

The torque required to product max tension without considering loses is 2.15 lbf-in. Giving an active tension control component of; $0.05 * \text{Max Tension Control Requirement} = .05 * 2.15 \text{ in lb} = 0.1075 \text{ lbf-in}$

With friction losses of $(6.53 \text{ lbf-in} - 2.15 \text{ lbf-in} = 4.38 \text{ lbf-in})$ 4.38 lbf-in we find that the output related to the losses is over 40 times the magnitude of the active tension control component output. $(4.38 \text{ lbf-in} / 0.1075 \text{ lbf-in}) = 40.74$

For effective tension control in the direct torque control mode, the active tension control torque signal component should be at least equal or greater to the torque required to overcome the gearbox losses.

Torque Ripple induced Tension Error

Another concern for effective tension control in the torque regulated modes is the tension error that can be caused from the motors inherent torque ripple when factored through the gearbox ratio. Synchronous servo motors can have a typical torque ripple from ~2.5% to < 1% of M0 or the rated motor torque. In this example, the motor selected has a rated torque of 11.5 lbf-in Considering a torque ripple of 2.5%, the ripple at the motor shaft will be $\sim .025 * 11.5 \text{ lbf-in} = .2875 \text{ lbf-in}$

This relates to $650/1 * .02875 \text{ lbf-in} = 186.875 \text{ lbf-in}$ on the output of the gearbox, and $186.875 \text{ lbf-in} / 10 \text{ in. (full roll radius)} = 18.687 \text{ lb. of open loop tension disturbance on the web at full roll.}$

Consider also how an oversized motor will add to the open loop tension error induced by the motor. Additionally, external web tension disturbances will also manifest through the system in the same manner.

Back-Driven Efficiency

High ratio gearing can have a much worse efficiency from the load side in comparison to the input that in effect isolates load changes from output shaft significantly.

Backlash and Compliance

Any lost motion between motor and load, be it backlash or compliance will have negative effects on the control of the load. Compliance can cause mechanical resonance that reduces servo response, and makes the system unstable and difficult to tune. Torsional compliance acts as a spring and also causes resonances. The larger the shaft diameter the stiffer or lower compliance it will have. The more mechanical sections, meaning couplings, gearbox stages, etc. in the system mean additional compliance and backlash.

Dynamic Performance

There are always disturbances in the system. They can come from torque ripple, out of round rolls, tuning, etc. It is possible for a system that is geared to match the lowest web speed to not have enough dynamic response to compensate for the natural disturbance.

Excess Output Torque from motor over sizing

As ratios increase, any additional torque in the selected motor size from optimal can raise the issue of too much output torque at the output of the gearbox. The outcome can be machine damage with web jams or web breaks. (In this example the motor torque requirement was 6.53 lbf-in and the selected motor was 10.5 lbf-in.)

An Alternative Solution

Utilizing the lowest possible gearbox ratios or if practical direct driven motors can help to eliminate the issues of load isolation through friction losses, reduce the losses to active tension control component, and reduce torque magnification.

Recommendations for gearing when required would be to consider an inline single stage planetary gearbox or timing belt. When considering a timing belt the limiting factor will be the distance between pulley centers. In most cases ratios in the range of 4:1 or less will be the maximum for timing belt gearing arrangements.

High resolution motor feedback encoders are the key to improving the low speed regulation of drive systems. With the introduction of the Sin/Cos optical encoders, feedback resolution has been increased from thousands of counts per motor revolution, to ~4 million counts per revolution for a 22 bit encoder to 16 million counts per revolution for 24 bit encoders. The higher the resolution of the motor feedback sensor, the lower the speed that the drive system can effectively regulate. The following table offers a rule of thumb for different encoder technologies and minimum regulated speed;

Table 1: Encoder Resolution / minimum speed regulation

Encoder Type	Minimum speed (Synchronous Motor)	
Resolver (16 Bit)	20.000	RPM
1024 Pulse HTL (Square Wave)	10.000	RPM
2048 Pulse HTL (Square Wave)	5.000	RPM
4096 Pulse HTL (Square Wave)	2.500	RPM
2048 Pulse Sin/Cos Encoder (22 bit)	0.250	RPM
8192 Pulse Sin/Cos Encoder (24 bit)	0.125	RPM

Considering the same reference specifications on a drive system with a low ratio single stage gearbox with a ratio of 6:1 we determine the following results;

$$\text{Max Speed at Core (RPM)} = \text{Maximum Web Speed} / ((\pi * \text{Core Diameter}^2) / 12) * \text{Gear Ratio}$$

$$12.00 \text{ fpm} / ((\pi * 6.75^2) / 12) * 6.00 = 40.74 \text{ RPM}$$

$$\text{Max Speed at Full roll (RPM)} = \text{Maximum Web Speed} / ((\pi * \text{Full Roll Diameter}^2) / 12) * \text{Gear Ratio}$$

$$12.00 \text{ fpm} / ((\pi * 20^2) / 12) * 6.00 = 13.75 \text{ RPM}$$

$$\text{Min Speed at Full roll (RPM)} = \text{Minimum Web Speed} / ((\pi * \text{Full Roll Diameter}^2) / 12) * \text{Gear Ratio}$$

$$0.10 \text{ fpm} / ((\pi * 20^2) / 12) * 6.00 = .29 \text{ RPM}$$

$$\text{Max Torque at Core (lbf-in)} = ((\text{Core Diameter} / 2) * (\text{Maximum Web Tension} / (\text{Gear Ratio} * \text{Gear Efficiency})))$$

$$((6.75^2 / 2) * (140 \text{ lb.} / (6 * 0.96))) = 82.03 \text{ lbf-in}$$

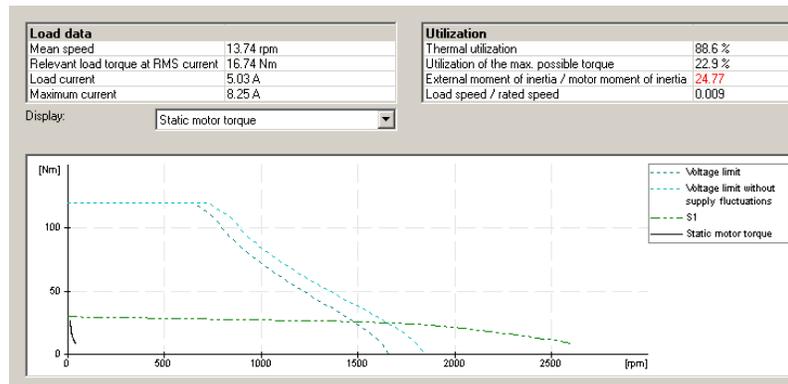
$$\text{Max Torque at Full Roll (lbf-in)} = ((\text{Full Roll Diameter} / 2) * (\text{Maximum Web Tension} / (\text{Gear Ratio} * \text{Gear Efficiency})))$$

$$((20^2 / 2) * (140 \text{ lb.} / (100 * 0.79))) = 243.06 \text{ lbf-in}$$

With these load criteria we can consider a synchronous motor with the minimum of 82.03 lbf-in of torque at the maximum speed at core (40.74 RPM) and 243.06 lbf-in of torque at minimum speed @ full roll (0.29 RPM).

Based on the data, we select a standard motor rated for (28Nm) 247.82 lbf-in of stall torque and (22.5Nm) 199.15 lbf-in at 2000RPM. See figure 8 for the selected motor / load curves.

Figure 8: Motor Selection / Load Requirements



The torque required to produce max tension without considering losses is 233.33 lbf-in. Giving an active tension control component of; $0.05 * \text{Max Tension Control Requirement} = .05 * 233.33 \text{ in lb} = 11.67 \text{ lbf-in}$

With friction losses of $(243.06 \text{ lbf-in} - 233.33 \text{ lbf-in} = 9.73 \text{ lbf-in})$, we find that the losses in this example are less than the magnitude of the active tension control component.

A motor is selected with a rated speed torque of (28Nm) 247.82 lbf-in Considering a torque ripple of 2.5% we find the ripple at the motor shaft to be $\sim .025 * 247.82 \text{ lbf-in} = 6.19 \text{ lbf-in}$

This relates to $6/1 * 6.19 \text{ lbf-in} = 37.17 \text{ lbf-in}$ on the output of the gearbox, and $37.17 / 10 \text{ in. (full roll radius)} = 3.72 \text{ lb.}$ of open loop tension disturbance on the web at full roll.

Selecting low ratio gearing with increased motor size offers a drive system with a higher level of inherent accuracy, and control dynamics. We have gone from a system that had a losses to active tension control component ratio of >40:1 to a system with a ratio of less than one. A system that inherently imparted disturbances of 18.687 lb. of open loop tension disturbance on the web at full roll to a system that offers 372 lb. of open loop tension disturbance on the web, five times less open loop tension disturbance.

Conclusions

Considering lowest practical gear ratio or if practical direct driven motors for web handling at very low web speeds can enhance machine tension control performance significantly by eliminating the issues of load isolation through friction losses, reduce the losses to active tension control component ratio, and reduce the torque ripple magnification.

In systems with lower to moderate power requirements the increased cost of the larger drive system in most cases will be offset by the reduced costs of the system gearing.

References

- [1] William Gilbert, "Motion Control for Converting", Aimcal Fall Conference, Charlotte, NC 2010.
- [2] Denis Morozov, "Optimizing Tension Control in Center-Driven Winders", ICE Conference, Orlando FL, 2010.